

GUROBI
OPTIMIZATION

Welcome to the Webinar

A Deep Dive into Advanced Analytics Model Review and Validation



- **Dr. Irv Lustig**

- Optimization Principal, Princeton Consultants
 - Lead Optimization Consulting Sales and Optimization Project Implementations
- Former Positions
 - CPLEX Optimization, Inc. Director of Numerical Optimization
 - ILOG, CPLEX Product Manager, eventually Vice President, ILOG Direct
 - IBM, Worldwide Optimization and Supply Chain Technical Sales Leader, then Manager of Optimization and Mathematical Software at IBM Research
- Ph.D. in Operations Research, Stanford University
 - Ph.D. Advisor: George Dantzig
- INFORMS Certified Analytics Professional



- **Ugo Feunekes, M.Sc.F**

- Co-Founder and CTO of Remsoft
 - Chief architect of Remsoft's suite of software
 - Leads Remsoft's research and development program and overall product development
- Holds Bachelors and Masters of Science in Forestry, as well as a Bachelors of Mathematics and Computer Science
- Experienced trainer and modeler with a depth of knowledge and experience in the realm of fire behavior, forest management, and asset lifecycle optimization.
- Edelman Laureate
 - *Taking the Politics out of Paving: Achieving Transportation Asset Management through O.R.* (2010)



About Princeton Consultants (www.princeton.com)



Princeton New Jersey

Information Technology & Management Consulting

Advanced Analytics *Strategy*
Application Development *Process Improvement*



Optimizing Performance



New York City

- **Stability:** over 35 years in business; over 1600 successful completed projects
- **Clients:** Industrial companies and their Logistics providers
- **Analytics-focused Professional Staff:** 85 full-time consultants, 2/3rds with graduate STEM degrees; plus network of top independent consultants and university professors. 50+ experienced data scientists/developers
- **Experience:** Senior Staff (top 28 consultants) average 15+ years experience; Firm Leadership (9 Directors) average 20+ years experience

Princeton Clients: Diversified Industries



Advanced Analytics Model Review & Validation

A Quality Assurance Service for Analytics Leaders

- **Validate and improve optimization and predictive models with an expert third party review**
 - Uncover new ideas for improvement
 - Benchmark your models and group against best practices
 - Give business leaders more confidence in your solutions
 - Help your specialists improve their development skills

Important Questions Addressed by Us

- What is a correct model?
 - What makes a model "correct"?
- What data is being integrated and how?
- How are solutions published and used in the business?
- What validation was done to see that the model met the needs of the business?
- How sensitive are the answers to the inputs?
- How often is the quality of models assessed, considering the changing nature of the data and the business?
- Did the implemented model reflect the intentions of the practitioner?
- Is data captured to allow models to be evaluated and tested outside of an operational system?
- If algorithms use random number generation techniques, are the random number sequences reproducible?

Engagement Summary



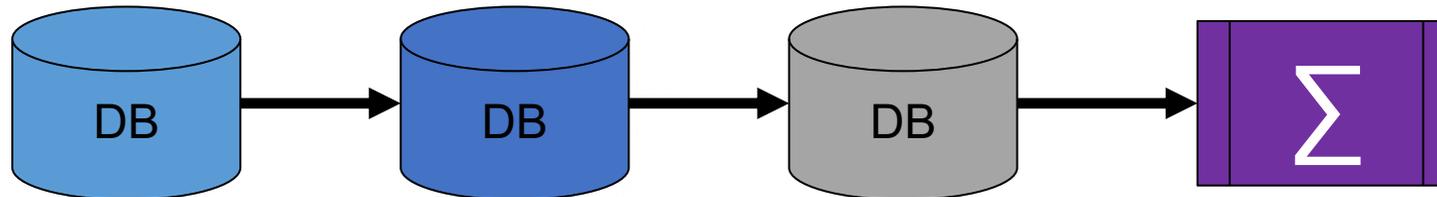
- Interview stakeholders from business and analytics development to understand business problem and context
- Review of existing models and procedures
- Review of data sources
- Implementation of models in alternative technologies to compare results
 - Languages, Solver, Analytics Engines
- Experiments with models to uncover issues
- Report of findings with suggestions for improvements and possible further investigation

Sample Optimization Questions

- If the problem has multiple optimal solutions, how does the chosen algorithm affect the variability in the answers?
- Could data be presented that would make the model infeasible?
- Are best practices followed for generating values passed to the model?
 - Precision vs. Accuracy
- If the solver is integrated into an application, have all appropriate exceptions been trapped?
- Were best practices observed to facilitate future model updates?
- Will the model scale as the dimensions of input data change?
- Is the underlying solver being used in the best way possible?
- For mixed integer programming, is pure optimality really needed?
- Would an alternate model yield better performance?

Understand how data feeds the system

- Two sources of data
 - Automatic feeds
 - Continually check the assumptions



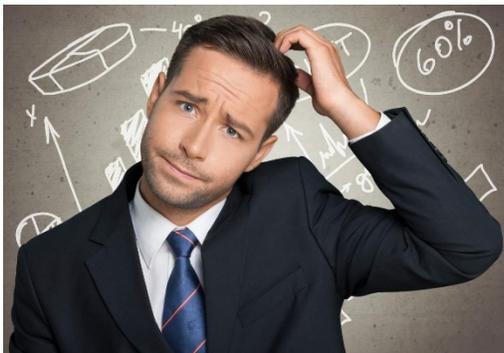
- User inputs
 - Create automatic alerts for data that falls outside control limits

Budget	\$40,500,000
Budget	\$50,400,300,200,000

It's All About the Data!

Problem: Users do not distinguish between bad data and bugs

- A bad recommendation means “it doesn’t work”
- Result: can’t verify; long validation cycles; frustration

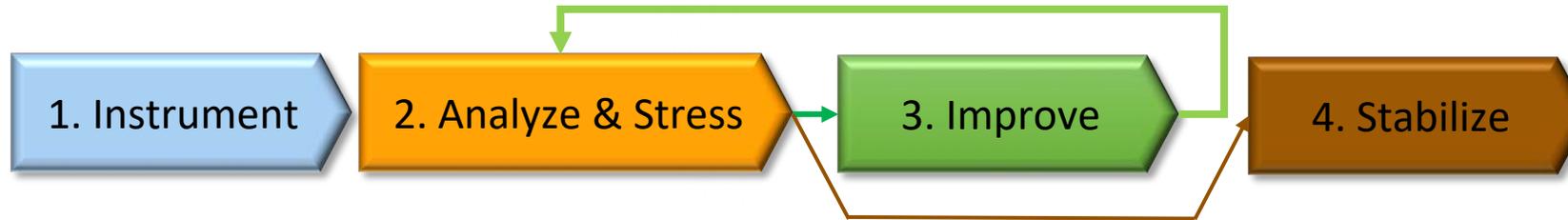


Solution: Data Cleaning is a core component of Optimization

- Clarity of “why” includes the incoming data
- Allow users to easily change the data where possible



Princeton Optimization Implementation Verification Methodology



- Create formal Optimization Algorithm Metrics (OAMs)

- Compute OAMs of current implementation
- Identify system failure and under-performance areas; Aggregate results; Compare to previous results
- Determine adversarial stress conditions

- Research and identify improvement strategies to algorithms
- Improve optimization solution quality, efficiency, robustness; Re-run

- Pass current implementation on for integration and testing
- Integrate implementation into application and processes for formal QA testing and production

- Build a simulator of data inputs
- Good simulation packages allow you to create graphical views of solutions that help end users validate the analytics
- Allows robust testing, especially with operational systems
 1. Validate data quality and completeness
 2. Iron out interface design kinks
 3. Fine tune the model
 4. Gain end user buy-in



informatics

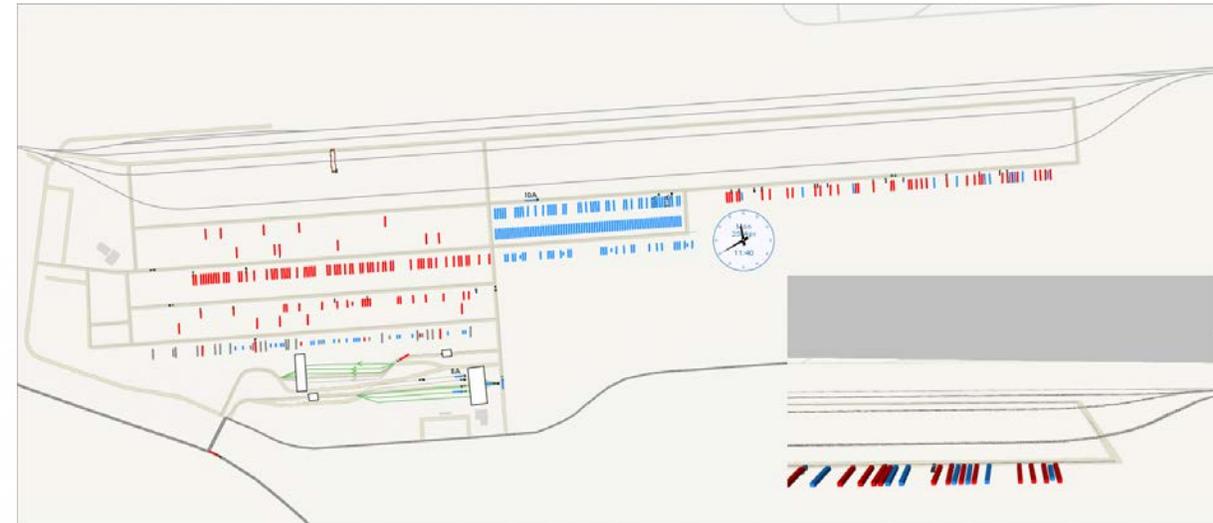
Why optimization models fail

How to avoid chaos in the field by combining simulation and optimization.



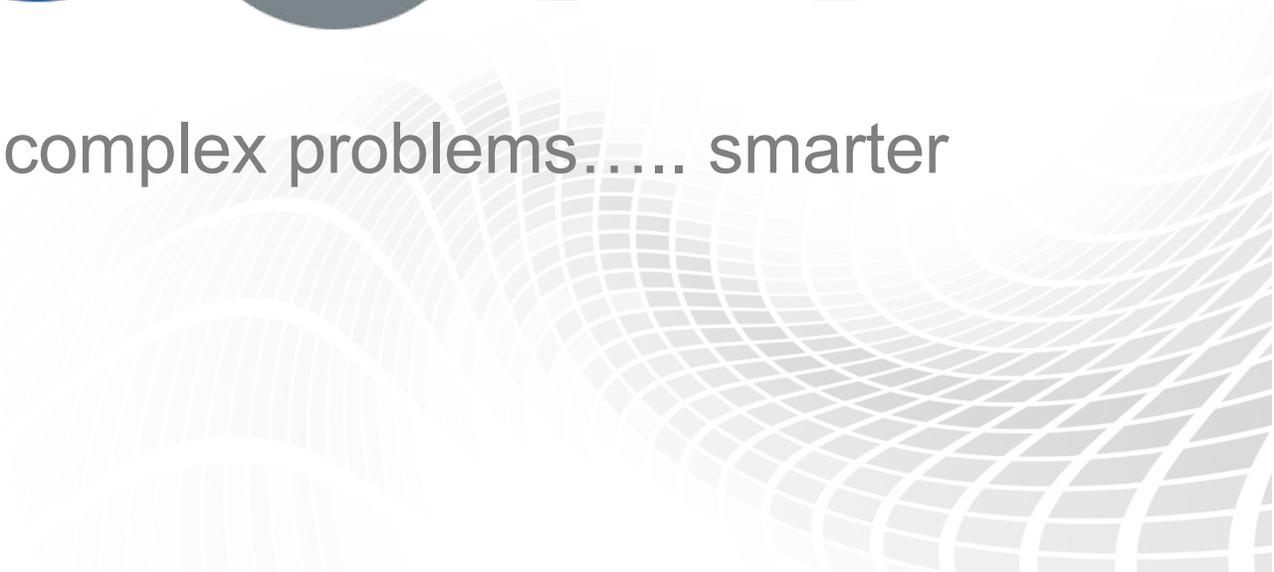
BY PATRICIA RANDALL

Analytics Magazine,
July/August, 2018



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- Continued development of cloud platform and SaaS products
 - Core IP & algorithms for modelling & optimization
- Systematic, Iterative Process to engage customers & proven implementation methodology



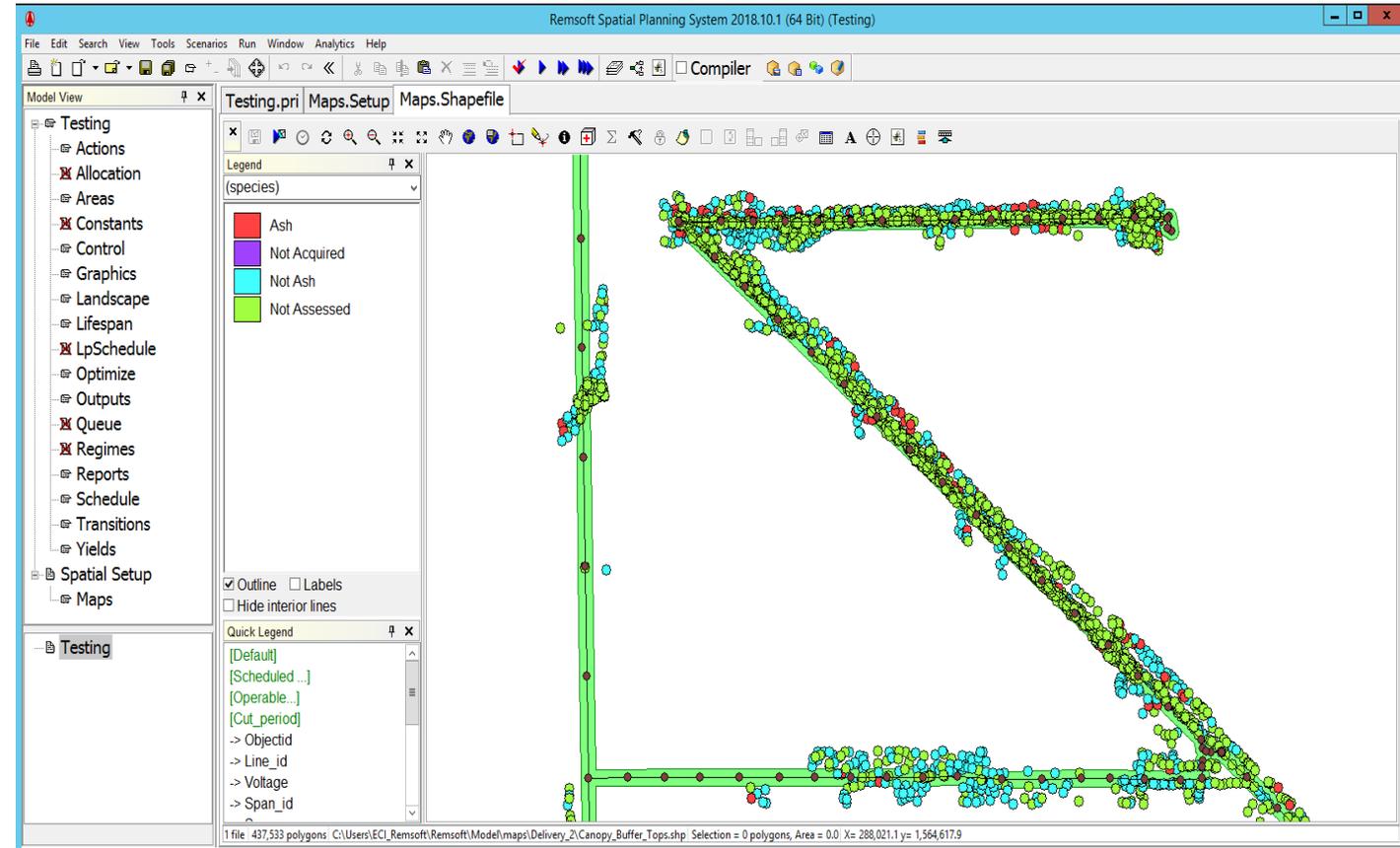


Remsoft Technology

Two advanced platforms for optimized planning and decision support

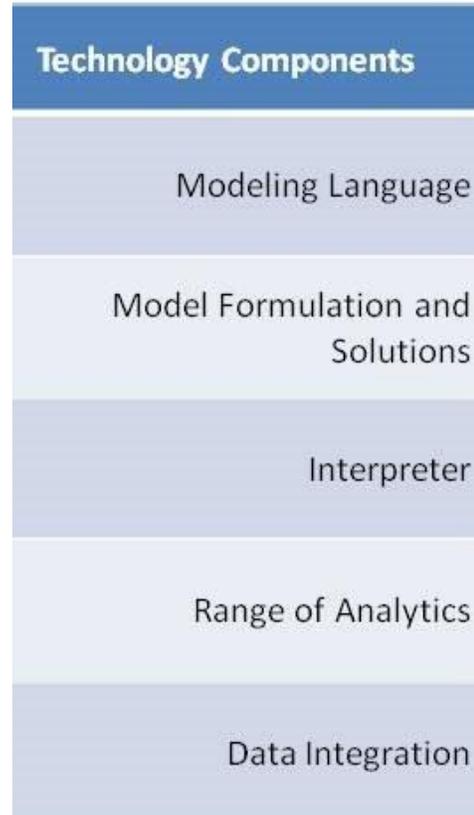
- Woodstock Modeling Platform for the desktop
- Remsoft Rise Platform for the cloud

Together they provide the foundation for all of our planning solutions.



Technology Components

- Modelling engine: syntax, editor, algorithms
- Allocation Optimizer: products to destinations
- Spatial Optimizer: spatial scheduling
- Regimes: Multi-period scheduling
- Solver (OEM)



Math for the masses

A user-defined means of representing a business or planning challenge in a structure suitable for modeling

A range of formulations & algorithms to solve the model:
Simulation: Deterministic, Binary Search, Monte Carlo
Optimization: LP, MIP, Goal Programming
Spatial Heuristics

Converts your modeling language (syntax) into a mathematical representation of the problem

Tools for testing, debugging and improving the model mapping, graphing, reporting

An open environment to connect to virtually any data source

Background

- Highly complex models, primarily MIP
 - Optimize a model with 944,490 rows, 4,765,013 columns and 24,439,033 nonzeros
 - Variable types: 4,578,017 continuous, 186,996 integer (0 binary)
- Wide ranging planning challenges
 - Crew scheduling
 - Transportation / Harvesting
 - Long term (100 year) sustainable forest/habitat management plan
- Frequent data refresh – even while building and testing models

The Issue

- Unreasonably long solve times
 - Days or longer when short term decisions are required
 - Frequent infeasibilities
- Unpredictable solve times
 - Different Gurobi tuning parameters required for different models – what works for one model does not work for another
 - Adding a single additional constraint makes solving impossible.... sometimes
- Client reluctant to simplify model or reduce constraints

Our question for Princeton Consultants:



What's happening? What is causing these issues?

- Are there things we could tweak in our modeling platform to improve solver performance?
- Are there better ways to structure some of these models?
- Can we improve Gurobi performance by changing parameters?
- Are there best practices you can share?

Precision vs. Accuracy

Standard Recommendation

- Use double precision in representing values for an application

Issue

- The double precision value may be too precise with respect to the business problem!

Example from Remsoft Application:

- Estimate amount of wood boards to 2 digits of accuracy after decimal point
- Multiply and divide by other data, such as rates and percentages to get hectares of forest
 - Could get a value such as 45.123456
- Constraint on hectares could be asking for accuracy down to the square micrometer!

Carefully consider the accuracy required in satisfying constraints, and possibly use less precision

- E.g., round numbers to 2 digits after decimal

Important to Consider when computing data and representing expressions related to money

- Do the constraints/objectives need accuracy to the pennies when values are in the millions of dollars?

Multiple Objectives

- Remsoft
 - Has the ability to specify “goals”
 - Customers typically used blended objectives
 - Blended objectives could be mixing different unrelated quantities
 - E.g. Costs in Dollars and Area in Hectares
 - Blended objectives can create numerical difficulties for solvers
 - Princeton recommended a hierarchical approach
- Gurobi supports multiple objectives
 - Two approaches
 - Blended
 - Hierarchical
- In general, Princeton finds that hierarchical approaches can more easily be mapped to business requirements

Constraint Violations and Normalizing Units

- Consider the following two constraints:
 - $X \geq 1500$
 $Y \geq 40$
- Remsoft system allows user to say these are soft constraints and solve by creating an objective that measures the total constraint violation
- If weighted equally, values of X and Y of 1490 and 30, respectively, are considered equal violations of the two constraints
- Might be better to normalize the constraints, and use a percent violation:
 - $X/1500 \geq 1$
 - $Y/40 \geq 1$
- Or appropriately weight the constraints in the penalty function

Modeling Recommendations: Add Extra Constraints



- For one MIP model, variables that were implicitly binary due to a combination of constraints were not declared as binary
- Gurobi Presolve did not figure out that those variables were supposed to be binary with the constraints as the model was formulated
- By specifying those variables to be binary, and creating additional constraints to link those binaries with other variables, Gurobi could branch on those variables and create stronger cuts
- Gurobi Presolve created a smaller problem, and solution times were significantly decreased (from hours to minutes)

- One Remsoft model had the following characteristics:
 - Binary decision variable $V(m, p)$ represents whether a machine m is used for work in period p .
 - Requirement that if machine m is used for work in period p , then at least n machines are used in that period, effectively:

$$\text{Machines}(p) = 0 \text{ OR } n \leq \text{Machines}(p) \leq n + 1$$

- Equivalent representation is
$$n V(m, p) \leq \text{Machines}(p)$$
$$\text{Machines}(p) \leq (n + 1)V(m, p)$$
- The variables $V(m, p)$ appear elsewhere in the model
- Model took many hours (overnight) to get any reasonable solution
- If $V(m, p)$ was relaxed to no longer be integer, Gurobi solved model to 1% gap in 39 minutes
- One can conclude that these variables are what make the problem difficult
- Leads to an alternate formulation of the model that introduces new variables and constraints that interact with the $V(m, p)$ variables that should generate stronger cuts for Gurobi

Following the engagement

Remsoft

- Made programming changes to address some of the rounding issues identified. Users now have the option to “turn on” this feature
- Increased model debugging tools to manipulate/analyse matrices
- Employed best practices for modeling both within our company and in the work we do with our clients
- Added Princeton recommendations to our model audit service

- Deployment of Optimization Models Requires
 - Optimization Modeling and Algorithmic expertise
 - Testing expertise
 - Software engineering expertise
- An independent review can assure that your models are delivering the value you expect
 - Deployment in real-time systems can be a challenge to get right
- What percentage of your models have errors??